Analysis of Model Predictive Control through a power converter in a renewable energy system

Imad A. Elzein
Belarusian national technical university
Department of Electrical and control engineering
Minsk, Belarus

Yury Petenko
Belarusian National Technical University
Department of electrical engineering
Minsk, Belarus

Abstract
Predictive control developments for applications in the field of renewable energy systems are still under investigation. In this article, the fundamentals of predictive control are studied with a focus on model predictive control (MPC). Based on this techniques, a control strategy for flexible power supply can be developed which could be implemented in renewable energy systems, such as solar photovoltaic (PV) systems.

1. Introduction
Renewable energy power is an important solution to global warming. Solar energy generated from PV systems is one of the fastest and the most promising growing renewable energy types. Recently more power electronics converters have been used to integrate the energy sources into the AC and/or DC common buses in a distributed generation (DG) system. As the penetration and capacities of DG units increase, the power converters are required to operate more efficiently and effectively to maintain high power quality and dynamic stability. To fulfil these requirements, advanced control techniques have been intensively investigated in the last years.

The main characteristic of predictive control is the use of the system model for the prediction of the controlled variables. Next, predefined optimized criterion selects the appropriate control set.

The predictive controller aims for system-level control using control horizons of several minutes or even hours, but it fails to consider the discrete-time models and behaviours of power converters that act as power electronic interface between the renewable energy sources and the grid. In this paper we extend and explore the feasibility of predictive control by suggesting appropriate control strategies for renewable energy systems.

2. Application of Predictive Control in Renewable Energy Systems
For PV system, several useful topologies have been studied and applied. Figure 1 shows a typical configuration of PV system where several strings are interfaced with their own DC-DC converter for voltage boosting and then connected to a common DC bus. After that, a common DC-AC inverter is used for grid interfacing. Usually the MPPT is implemented on the DC-DC converter, while the grid synchronization and power regulation are achieved by the grid-side inverter.

![Figure 1. A typical configuration of PV system.](image)

In this paper we concentrate on the control of the grid-side common inverter of the PV system (figure 1). Grid-connected PV systems should be controlled to regulate active and reactive powers flexibly for voltage support and power quality improvement. In this sense, flexible power regulation capability for a DG unit becomes more and more significant. For two-level inverters, there are eight possible voltage vectors generated by the inverter (six active vectors and two null vectors), and the α-β plane is divided into six sectors, as shown in Figure 2.

![Figure 2. Possible voltage vectors generated by the inverter and sector division](image)
According to the equivalent circuit in Figure 1, the system mathematical model can be expressed as:

\[ V_i = V_e + IR + L \frac{dI}{dt} \] (1)

where \( V_i \) and \( V_g \) are the inverter output voltage vector and grid voltage vector, respectively; \( I \) the line current vector; \( L \) the filter inductance; \( R \) the filter resistance. The instantaneous active and reactive powers exchanged between the PV and the utility grid can be expressed as:

\[ P = \frac{3}{2} \text{Re}\{V_e I^*\} = \frac{3}{2} (V_{ge} I_a + V_{gb} I_b) \] (2)

\[ Q = \frac{3}{2} \text{Im}\{V_e I^*\} = \frac{3}{2} (V_{gb} I_a - V_{ge} I_b) \] (3)

where \( a \) and \( b \) represent the real and imaginary components of the space vector expressed in the stationary frame. According to Equations (2) and (3), the active and reactive power derivatives can be calculated as:

\[ \frac{dP}{dt} = \frac{3}{2} \left( \frac{dV_{ge}}{dt} I_a + V_{gb} \frac{dI_a}{dt} + \frac{dV_{gb}}{dt} I_b - V_{ge} \frac{dI_b}{dt} \right) \] (4)

\[ \frac{dQ}{dt} = \frac{3}{2} \left( \frac{dV_{gb}}{dt} I_a + V_{ge} \frac{dI_a}{dt} - \frac{dV_{ge}}{dt} I_b - V_{gb} \frac{dI_b}{dt} \right) \] (5)

Considering sinusoidal and balanced line voltage, one can obtain:

\[ \frac{dV_{gb}}{dt} = -\omega_b \cdot V_{gb} \] (6)

\[ \frac{dV_{ge}}{dt} = \omega_a \cdot V_{ge} \] (7)

Thus, the inverter output active and reactive power derivatives can be obtained by substituting Equations (1), (6) and (7) into Equations (4) and (5) as:

\[ \frac{dP}{dt} = \frac{R}{L} P - \omega Q + \frac{3}{2L} \left( \text{Re}(V_e V_i^*) - |V_e|^2 \right) \] (8)

\[ \frac{dQ}{dt} = \omega P - \frac{R}{L} Q + \frac{3}{2L} \text{Im}(V_e V_i^*) \] (9)

\[ p^{k+1} = T_e \left[ -\frac{R}{L} P - \omega Q + \frac{3}{2L} \left( \text{Re}(V_e V_i^*) - |V_e|^2 \right) \right] + p^k \] (10)

\[ q^{k+1} = T_e \left[ \omega P - \frac{R}{L} Q + \frac{3}{2L} \text{Im}(V_e V_i^*) \right] + q^k \] (11)

Now the predictive model has been obtained mathematically with Equations (10) and (11). Figure 3 depicts the block diagram of the proposed MPC strategy for grid-connected PV systems. After the power is predicted, the next step is to evaluate the effects of each voltage vector on active and reactive powers and then select the one producing the least power ripple according to a specific cost function. Here, the cost function is defined as follows considering the same weighting priority for \( P \) and \( Q \):

\[ J = (P^* - p^{k+1})^2 + (Q^* - q^{k+1})^2 \] (12)

Once the optimal voltage vector is determined, it will be applied during the next sampling period to control the inverter.

**Figure 3. Block diagram of MPC strategy of PV systems.**

**Conclusions**

This paper has reviewed the most important type of predictive control approaches, namely model predictive control which can be employed in renewable energy systems such as PV power generation. Application example has been described. With the increasing level of renewable energy sources penetration in existing power system, new challenges have been posted to the control of these distributed generation units (DGs). The DGs are not only controlled to injected power into the main grid, also required to participate in grid support by flexible power regulation.